

# First principle study on structural, elastic and electronic properties of cubic BiFeO<sub>3</sub>

M.K. Yaakob<sup>a,b</sup>, M.F.M. Taib<sup>a,b</sup>, M.S.M. Deni<sup>a,b</sup>, Amreesh Chandra<sup>c</sup>,  
L. Lu<sup>d</sup>, M.Z.A. Yahya<sup>b,e,\*</sup>

<sup>a</sup>Faculty of Applied Sciences, Universiti Teknologi MARA, 40450 Shah Alam, Malaysia

<sup>b</sup>Ionics Materials & Devices (iMADE) Research Laboratory, Universiti Teknologi MARA, 40450 Shah Alam, Malaysia

<sup>c</sup>Department of Physics and Meteorology, Indian Institute of Technology, Kharagpur-721302, India

<sup>d</sup>Department of Mechanical Engineering, National University of Singapore, 10 Kent Ridge Crescent, Singapore 119260, Singapore

<sup>e</sup>Faculty of Science and Defence Technology, National Defence University of Malaysia, 57000 Kuala Lumpur, Malaysia

Available online 16 October 2012

## Abstract

We present the first principle studies of the structural and electronic properties in high temperature cubic phase (Pm3m) of BiFeO<sub>3</sub> based on Density Functional Theory (DFT). All calculations are performed within Local Density Approximation (LDA) functional and Generalized Gradient Approximation (GGA) functional with Ultrasoft Pseudopotentials (USP). It shows that the calculated structural parameters of cubic BiFeO<sub>3</sub> are in a good agreement with previous literatures. Based on the calculated of elastic properties of cubic BiFeO<sub>3</sub>, this material shows a stable mechanical structure. In electronic band structure, the electron wave propagates through Brillouin zone X–R–M–G–R points where the highest valence band overlap with the lowest conduction band to give zero energy band gaps. The Density of States (DOS) demonstrated the significant hybridization between Bi6p, Fe3d and O2p in the range of –5 eV–5 eV. Thus, it can be implied that multiferroic BiFeO<sub>3</sub> are metallic at cubic phase and the metal–insulator transition in this material obeys the band theory.

© 2012 Elsevier Ltd and Techna Group S.r.l. All rights reserved.

**Keywords:** Multiferroic; BiFeO<sub>3</sub>; Density Functional Theory (DFT)

## 1. Introduction

Multiferroic BiFeO<sub>3</sub> (BFO) has attracted a new interest in fundamental sciences and has shown great potential for a new application due to its ability to exhibit both ferromagnetic (G-type antiferromagnetic) and ferroelectric properties at room temperature [1]. In recent year, the first principle and experimental studies focus on this essential multiferroic material due to their superior in ferroelectric properties and room temperature magnetoelectric effect have been carried out [2–4]. However, there are very few literature studies on high temperature phase transition (paraelectric  $\gamma$ -phase) [5,6]. As BFO decomposed at high temperature, the study on phase and metal–insulator tran-

sitions at high temperature become almost impossible [1]. Moreover, there is very little report on first principle study of cubic Pm3m BiFeO<sub>3</sub>. Therefore, the paraelectric–ferroelectric transition and metal–insulator transition in this material are still not fully understood.

In this work, we study on structural, elastic and electronic properties of BFO in paraelectric Pm3m cubic phase by First Principle method (which can only be experimentally obtained at high temperature). The origin and metal–insulator transition of multiferroic BFO materials will be discussed in detail using electronic ground states calculation.

## 2. First principle method

The first principle calculations of paraelectric cubic (Pm3m space) BiFeO<sub>3</sub> materials (shown in Fig. 1) have been performed by using the Cambridge Serial Total

\*Corresponding author at: National Defence University of Malaysia, 57000 Kuala Lumpur, Malaysia.

E-mail address: [mzayahya@yahoo.com](mailto:mzayahya@yahoo.com) (M.Z.A. Yahya).

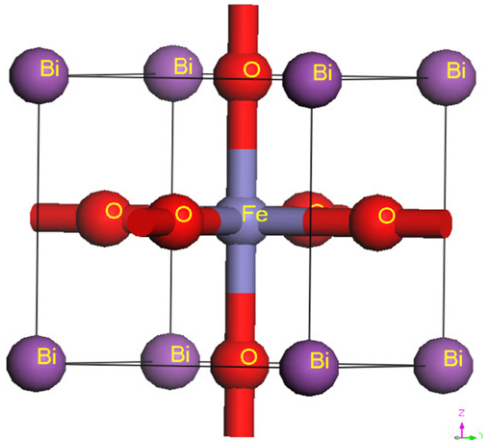


Fig. 1. Schematic diagram of cubic (Pm3m space group) BiFeO<sub>3</sub> with perovskite structure.

Energy Package (CASTEP) package [7,8] with Plane Wave Basis sets and Vanderbilt Ultrasoft Pseudopotentials (USP) [9]. This first principle calculation is based on Density Functional Theory (DFT) within Local Density Approximation (LDA) [10] and Generalized Gradient Approximation (GGA) [11] with and without of spin polarized. In this work, the geometry optimization calculation is achieved using convergence thresholds of  $5.0 \times 10^{-6}$  eV/atom for total energy, 0.01 eV/Å for maximum force, 0.02 GPa for pressure and  $5.0 \times 10^{-4}$  Å for displacement. The electronic properties calculation were performed with and without Hubbard U interaction LDA and corrected LSDA + U (U = 3 eV) functionals.

### 3. Results and discussion

In this work, geometry optimization of Pm3m cubic phase BFO was performed within LDA and different GGA (PBE, PW91 and WC) functional with and without of spin polarized. The comparison is listed in Table 1 and it shows that the calculated lattice parameter is comparable to the other previous first principle study [4] and in good agreement with experimental data [6,12]. The different between the calculation data and experimental data is believed to have come from the defects and the limitation in high temperature measurement of the experimental study. From the comparison, the geometrical optimization calculation of cubic BFO with spin polarized show better results than without spin polarized.

Table 2 shows the calculated Single-crystal elastic constant ( $C_{ij}$ ), Bulk modulus ( $B_0$ ), optimum volume ( $V_0$ ), Young modulus ( $E$ ) and polycrystalline aggregate properties of cubic BFO. The calculations are performed within LDA and GGA-PBE functional with spin polarized. The elastic study of material is important for both fundamental and application of materials science. From our calculated result, it clearly shows that the elastic properties of cubic BFO increased with decreasing of the optimum volume. In cubic materials, the mechanical stability of the crystal is presented

Table 1

Structural lattice parameter of cubic BiFeO<sub>3</sub> calculated from LDA and different GGA functional. Previous theoretical and experimental data also included for comparison.

	$a$ (Å)	
	Spin polarized	Non-spin polarized
LDA	3.844	3.699
GGA-PBE	3.946	3.804
GGA-PW91	3.943	3.805
GGA-WC	3.907	3.770
Exp.	3.9916 <sup>a</sup> 3.93 <sup>b</sup>	
Theoretical	3.75(LDA) <sup>c</sup> 4.21(GGA) <sup>c</sup>	

<sup>a</sup>Reference [6].

<sup>b</sup>Reference [12].

<sup>c</sup>Reference [4].

Table 2

Single-crystal elastic constant ( $C_{ij}$ ), Bulk modulus ( $B_0$ ), optimum volume ( $V_0$ ), Young modulus ( $E$ ), polycrystalline aggregate properties of bulk modulus ( $B$ ), shear modulus ( $G$ ) in Voigt–Reuss–Hill approaches of cubic BiFeO<sub>3</sub> calculated from local (LDA) and non-local (GGA) functional with spin polarized.

Property	With spin polarized	
	LDA	GGA-PBE
$V_0$ (Å <sup>3</sup> )	56.79	61.44
$C_{11}$ (GPa)	$296.4 \pm 5.3$	$238.5 \pm 10.6$
$C_{12}$ (GPa)	$111.9 \pm 11.2$	$104.7 \pm 1.4$
$C_{44}$ (GPa)	$62.2 \pm 0.9$	$62.0 \pm 3.7$
$B_0$ (GPa)	$173.4 \pm 7.7$	$149.3 \pm 3.6$
$B_V$ (GPa)	173.4	149.3
$B_R$ (GPa)	173.4	149.3
$B_H$ (GPa)	173.4	149.3
$E$ (GPa)	235.1	174.6
$G_V$ (GPa)	74.3	64.0
$G_R$ (GPa)	71.6	63.9
$G_H$ (GPa)	72.9	63.9

by several criteria [13]:  $(C_{11} - C_{12}) > 0$ ;  $(C_{11} + 2C_{12}) > 0$ ;  $C_{44} > 0$ . The calculated elastic constants of cubic BFO show positive values and it is suggested to have a stable mechanical structure. The bulk modulus ( $B_{V,R,H}$ ) and shear modulus ( $G_{V,R,H}$ ) represent the calculated results pertaining to Voigt–Reuss–Hill approaches [14]. It is noted that for any cubic phase, the Voigt–Reuss–Hill bulk moduli are identical. This elastic properties study also can provide valuable theoretical information on mechanical properties of the material. For deeper understanding on the origin and metal–insulator transition in BFO material, we carried out the electronic ground states properties calculation by using first principle method within LDA (non-spin paramagnetic) and LSDA + U (U = 2 eV). Based on the first principle study [16], energy U = 2 eV is efficient to give rhombohedral R3c BFO in insulator with correct electron occupied orbitals.

The electron waves propagate in band structure through Brillouin zone X–R–M–G–R points and density of states

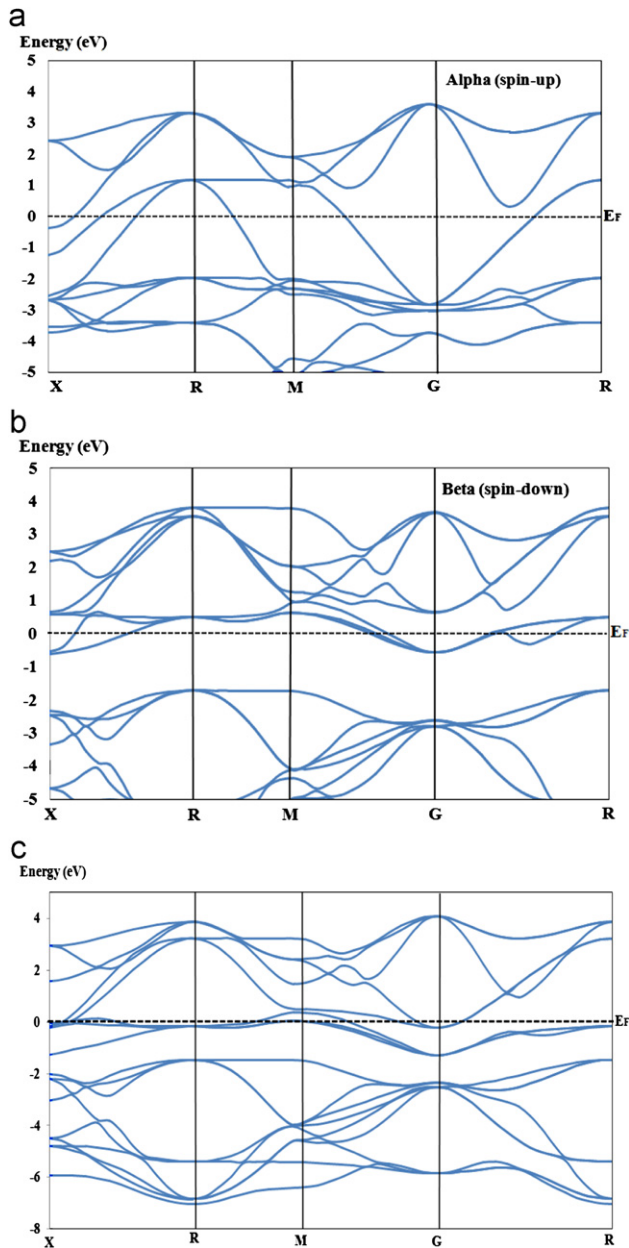


Fig. 2. Electronic band structure for alpha states (spin-up) (a), beta states (spin-down) (b) and non-magnetic and (c) of cubic  $\text{BiFeO}_3$  along the high symmetry axes of the Brillouin zone.

(DOS) of cubic BFO is shown in Figs. 2 and 3 respectively. The Fermi energy in this calculation is set to zero energy. From the calculated band structure (LDA and LSDA+U), BFO in  $\text{Pm}\bar{3}\text{m}$  cubic phase has zero energy band gaps (metallic) which the highest valence band overlaps with the lowest conduction band.

It is obviously shown that electron waves propagate from the highest valence band through X–R–M–G points and overlap with the lowest conduction band to leave BFO metallic material in cubic phase. Thus, the metal–insulator in this material obeys the band theory instead of Mott theory due to its transition that is related to the change in their structure [6,15]. The correlation between

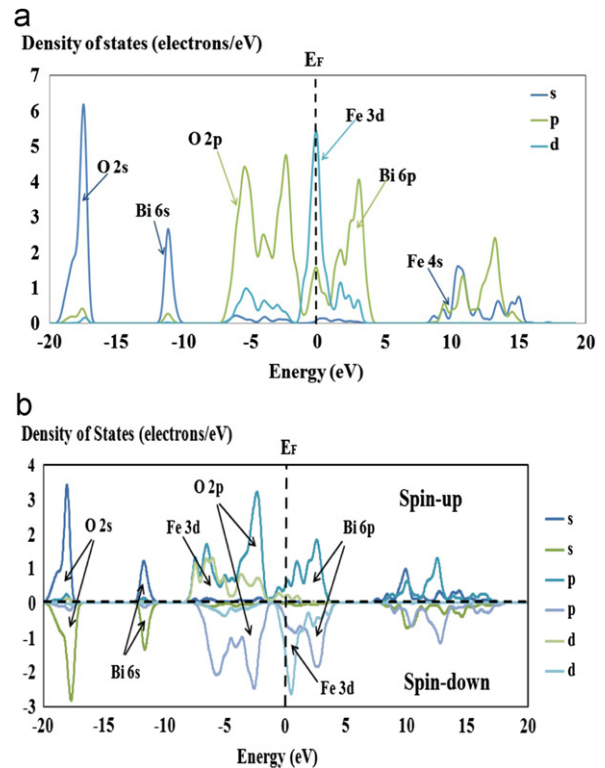


Fig. 3. Density of states (DOS) for LDA calculation (a) and LSDA (spin-up and spin-down states) calculation (b) of cubic  $\text{Pm}\bar{3}\text{m}$   $\text{BiFeO}_3$ .

electron occupied orbital with the band structure (valence band and conduction band) is illustrated by DOS calculation (see Fig. 2). Our DOS calculation shows that the valence band and conduction band are occupied with O2p, Fe3d and Bi6p states respectively with significant hybridization between Bi6p, Fe3d and O2p states in the range of  $-5\text{ eV}$ – $5\text{ eV}$ . Hence, the hybridization of Bi6p–O2p states in addition of Bi6s states in DOS demonstrated the lone-pair of  $\text{Bi}^{3+}$  cation (stereochemically active  $6s^2$  lone-pair) that has possibly contributed to the large ferroelectric polarization in the BFO material [16,17].

#### 4. Conclusion

The structural and electronic properties of multiferroic BFO at high temperature cubic phase are systematically studied by first principle study based on DFT (in CASTEP package). The calculated structural properties with LDA and GGA (PBE, PW91 and WC) calculations are in good agreement to the other previous experiment and first principle studies. Based on our first principle investigation, BFO is a metallic material in  $\text{Pm}\bar{3}\text{m}$  cubic phase which corresponds to the zero band gap in band structure calculation. The results obtained are in agreement with experimental study by Palai et al. [6]. We suggest that the metal–insulator transition in BFO material obeys the band theory instead of Mott theory. The strong Coulomb repulsive force due to the hybridization of Bi6p–O2p states

has contributed large ferroelectric polarization in this multiferroic material.

### Acknowledgment

This work is supported by the Fundamental Research Grant Scheme [Grant no. 600-RMI/ST/FRGS 5/3/Fst (4/2010)] provided by the Ministry of Higher Education and the Institute of Science (IOS), Universiti Teknologi MARA, Malaysia.

### References

- [1] G. Catalan, J.F. Scott, Physics and applications of bismuth ferrite, *Advanced Materials* 21 (2009) 2463–2485.
- [2] A.Y. Kim, S.H. Han, H.W. Kang, H.G. Lee, J.S. Kim, C.I. Cheon, Dielectric and magnetic properties of BiFeO<sub>3</sub> ceramics prepared by hydrothermal synthesis, *Ceramics International* 38 (2012) 397–401.
- [3] K. Liu, H. Fan, P. Ren, C. Yang, Structural, electronic and optical properties of BiFeO<sub>3</sub> by first principle, *Journal of Alloys and Compounds* 509 (2011) 1901–1905.
- [4] D. Bensaid, N.E. Benkhetou, A. Kourdassi, Structural and electronic properties of BiXO<sub>3</sub> (X=Mn, Fe, Cr), *Journal of Modern Physics* 2 (2011) 642–650.
- [5] E.P. Smirnova, A. Sotnikov, S. Ktitorov, N. Zaitseva, H. Schmidt, M. Weihnacht, Acoustic properties of multiferroic BiFeO<sub>3</sub> over the temperature range 4.2–830 K, *European Physical Journal B* 83 (2011) 39–45.
- [6] R. Palai, R.S. Katiyar, H. Schmid, P. Tissot, S.J. Clark, J. Robertson, S.A.T. Redfern, J.F. Scott, The  $\beta$  phase of multiferroic bismuth ferrite and its  $\gamma$ - $\beta$  metal-insulator transition, *Physical Review B* 77 (2008) 014110.
- [7] S.J. Clark, M.D. Segall, C.J. Pickard, P.J. Hasnip, M.J. Probert, K. Refson, M.C. Payne, First principle method using CASTEP, *Zeitschrift Fur Kristallographie* 220 (2005) 567–570.
- [8] K. Refson, S.J. Clark, P.R. Tulip, Variational density functional perturbation theory for dielectric and lattice dynamics, *Physical Review B* 73 (2006) 155114.
- [9] D. Vanderbilt, Soft self-consistent pse-udopotentials in a generalized eigenvalue formulism, *Physical Review B* 41 (1990) 7892–7895.
- [10] R.E. Cohen, H. Krakauer, Lattice dynamics and origin of ferroelectricity in barium titanate, *Physical Review B* 42 (1990) 6416–6423.
- [11] J.P. Perdew, J.A. Chevary, S.H. Vosko, K.A. Jackson, M.R. Pederson, D.J. Singh, C. Fiolhais, Atoms, molecules, solids, and surfaces: applications of the generalized gradient approximation for exchange and correlation, *Physical Review B* 46 (1992) 6671–6687.
- [12] F. Sugawara, S. Iida, Y. Syono, S. Akimoto, Magnetic properties and crystal distortions of BiMnO<sub>3</sub> and BiCrO<sub>3</sub>, *Journal Physical Society* 25 (1968) 1553.
- [13] J. Wang, S. Yip, S.R. Phillpot, D. Wolf, Crystal instabilities at finite strain, *Physical Review Letters* 71 (1993) 4182.
- [14] G. Simmons, H. Wang, in: *Single Crystal Elastic Constants and Calculated Aggregate Properties: A Handbook*, second ed., The MIT Press, Cambridge, 1971.
- [15] A.G. Gavriliuk, V.V. Struzhkin, I.S. Lyubutin, S.G. Ovchinnikov, M.Y. Hu, P. Chow, Another mechanism for the insulator-metal transition observed in mott insulators, *Physical Review B* 77 (2008) 155112.
- [16] A.N. Hill, P. Battig, C. Daul, First principles search for multiferroism in BiCrO<sub>3</sub>, *Journal of Physical Chemistry B* 106 (2002) 3383–3388.
- [17] J.B. Neaton, C. Ederer, U.V. Waghmare, N.A. Spaldin, K.M. Rabe, First principles study of spontaneous polarization in multiferroic BiFeO<sub>3</sub>, *Physical Review B* 71 (2005) 014113.